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## Spectroscopy of $Gd^{3+}$ in $KYF_4$ : a system with several luminescent sites

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**Abstract.** The spectroscopy of  $Gd^{3+}$  in  $KYF_4$  is reported. Evidence is given that there are two different classes of luminescent sites: classes I and II. The positions of the crystal field components of the  ${}^6P_{7/2}$  and  ${}^6I_{7/2}$  term levels are presented. The radiative transition probabilities for the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition are derived, for both classes, from decay measurements and spectral intensity measurements. At 4.2 K energy transfer occurs from class I to class II. Above 25 K energy transfer also occurs from class II to class I.

### 1. Introduction

Rare earth fluorides are important materials. Due to their chemical and physical properties they are advantageous materials for application in laser systems. Several reviews exist on the chemistry of the rare earth fluorides [1, 2]. Among the fluorides,  $KYF_4$  has been classified as a prospective laser material [3]; in fact,  $KYF_4$  doped with  $Nd^{3+}$  has been shown to be a promising laser material [4].

In this article we study the spectroscopic properties of  $KYF_4$  doped with 5 at.%  $Gd^{3+}$ . The positions of the lowest term levels are presented. It is shown that there are two different classes of luminescent sites, which are labelled class I and class II. The liquid helium temperature values of the transition probabilities of transitions starting at the lowest crystal field components of the  ${}^6P_{7/2}$  and the  ${}^6I_{7/2}$  term levels are derived from the spectral data and decay measurements. At 4.2 K energy transfer occurs from class I to class II. Above 25 K energy transfer occurs also from class II to class I.

### 2. Experimental details

#### 2.1. Sample preparation

The crystals were grown by hydrothermal synthesis. The size of the crystals is about 4 mm × 3 mm × 3 mm. The optical quality is good: the crystals are colourless and fully transparent. According to Greis and Haschke,  $KYF_4$  is isostructural with  $KErF_4$  ([2] and references therein). The structural analysis of  $KErF_4$  has been performed by Aleonard *et al* [5]. This structure is related to the fluorite structure [2, 5]. The

hexagonal unit cell contains three cation layers, stacked according the sequence 'abc'. In each layer there are twelve cation positions. Four of these positions are occupied by  $Y^{3+}$  in each layer. Another four positions are occupied by either  $Y^{3+}$  or  $K^+$ , according to a statistical distribution of four  $Y^{3+}$  ions and eight  $K^+$  ions over the three layers. The last four positions are also occupied by either  $Y^{3+}$  or  $K^+$ , according to a statistical distribution of two  $Y^{3+}$  ions and ten  $K^+$  ions over the three layers. The space group of the unit cell is  $P3_112$  [5]. None of the cation positions has inversion symmetry [6].

The concentration of  $Gd^{3+}$  is 5 at. %.

## 2.2. Optical instrumentation

The measurements are performed with a frequency-doubled dye laser, pumped by a Nd-YAG laser (for details see [7]). The monochromator is a Spex 1269. Low resolution spectra are measured with a Perkin-Elmer MPF 44-B spectrofluorometer described in detail in [8]. During the measurements the temperature of the sample can be varied between 1.5 and 300 K.

## 3. Results

After laser excitation at 4.2 K at  $35741\text{ cm}^{-1}$ , the lowest  ${}^6I_{7/2}$  crystal field (CF) component, emission is observed in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition region (figure 1). The emission maxima are at  $31987$  and  $32070\text{ cm}^{-1}$ . The emission line at  $31987\text{ cm}^{-1}$  shows a pronounced shoulder on the higher energy side. We will not distinguish the shoulder from the main line for reasons mentioned later. After excitation into one of the higher  ${}^6I_{7/2}$  CF components, at  $35878\text{ cm}^{-1}$ , emission can also be observed in the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  region. The maxima are at  $35702$  and  $35741\text{ cm}^{-1}$  (figure 2). The energy difference between the maxima is  $83$  and  $39\text{ cm}^{-1}$  in figures 1 and 2, respectively. These values are too large to ascribe the occurrence of more than one line in figures 1 and 2 to a thermal population of the higher crystal field components of the  ${}^6P_{7/2}$  and  ${}^6I_{7/2}$  term levels, respectively. The linewidths of the emission lines are  $\approx 13\text{ cm}^{-1}$  for the lines at  $32070$  (figure 1) and  $35741\text{ cm}^{-1}$  (figure 2) and  $\approx 20\text{ cm}^{-1}$  for the lines at  $31987$  (figure 1) and  $35702\text{ cm}^{-1}$  (figure 2). This is much larger than the linewidths of the corresponding transitions of  $Gd^{3+}$  in the crystalline powders of  $LaF_3$  and  $LiYF_4$  [9] and in the single crystal  $Cs_2NaGdCl_6$  [10, 11], namely  $\approx 5\text{ cm}^{-1}$ . Therefore, we conclude that there are two classes of sites for the  $Gd^{3+}$  ion, which give rise to different energy level schemes. Each of the classes shows a considerable inhomogeneous broadening due to the statistical distribution of  $Y^{3+}$  and  $K^+$  over the cation positions. The classes are labelled I and II as in figure 1.

The assignment of two classes is confirmed by the excitation spectra of the different emission lines. The excitation spectra in the  ${}^8S_{7/2} \rightarrow {}^6P_{7/2}$  region are given in figure 3. The excitation spectrum of the emission line at  $31987\text{ cm}^{-1}$  (class II) shows at least six lines (figure 3(b)). For a  $Gd^{3+}$  ion on a site without inversion symmetry the  ${}^6P_{7/2}$  term level is expected to split into four CF components. Three of the lines, however, are also present in the excitation spectrum of the emission line at  $32070\text{ cm}^{-1}$  (class I) (figure 3(a)). Therefore, we conclude that at 4.2 K energy transfer occurs from class I to class II, but not vice versa. A comparison of the two excitation spectra allows an assignment of the lines to the different CF components of the  ${}^6P_{7/2}$  term level of  $Gd^{3+}$

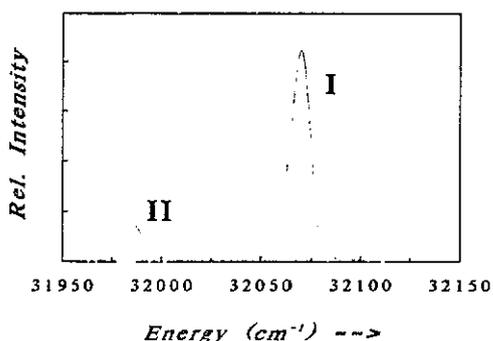


Figure 1. Emission spectrum in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  region of  $Gd^{3+}$  in  $KYF_4$  at 4.2 K. Excitation at  $35741\text{ cm}^{-1}$ . The labels 'I' and 'II' define the class of site numbering.

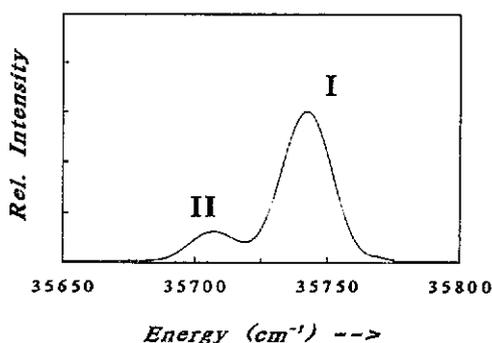


Figure 2. Emission spectrum in the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  region of  $Gd^{3+}$  in  $KYF_4$  at 4.2 K. Excitation is at  $35878\text{ cm}^{-1}$ . The labels 'I' and 'II' indicate the class of sites.

in class I and class II as in figure 3. Lines occurring in both spectra are assigned to the CF components of the  ${}^6P_{7/2}$  term level of  $Gd^{3+}$  in class I. The remaining lines in figure 3(b) are assigned to the CF components of the  ${}^6P_{7/2}$  term level of  $Gd^{3+}$  in class II. The positions and assignments are tabulated in table 1. The total CF splitting of the  ${}^6P_{7/2}$  term level of class I is estimated to be  $84\text{ cm}^{-1}$ ; the CF splitting of class II yields  $167\text{ cm}^{-1}$ .

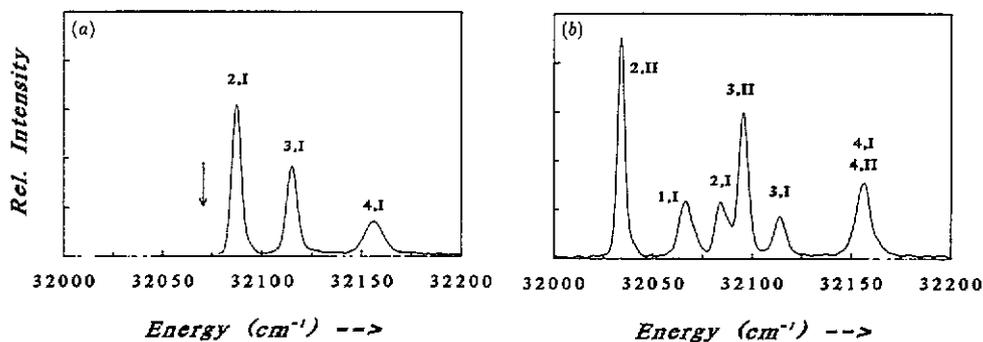


Figure 3. Excitation spectrum in the  ${}^8S_{7/2} \rightarrow {}^6P_{7/2}$  region of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition of the two classes of sites of  $Gd^{3+}$  in  $KYF_4$  at 4.2 K. (a) is for emission from class I. The arrow indicates the position of the monitored emission line. (b) is for emission from class II. The differences in intensity of the lines in (a) and (b) allow an assignment of the lines to class I or II. The lines are labelled with the CF component index and the class number.

The excitation spectrum of the emission at  $32005\text{ cm}^{-1}$ , i.e. the shoulder mentioned earlier, does not differ from the excitation spectrum of the main  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission line of class II (at  $31987\text{ cm}^{-1}$ ). We therefore also classify the shoulder as class II emission.

Table 1. Data on the  $Gd^{3+}$  spectroscopy in  $KYF_4$ . Two classes of sites are observed (I and II). For both classes the following results are given: the positions of the  ${}^6P_{7/2}$  and  ${}^6I_{7/2}$  CF components, the ratio  $r$  of the vibronic intensity to the zero-phonon intensity for the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition, and the transition probabilities at 4.2 K. The radiative transitions are to the  ${}^8S_{7/2}$  ground state, whereas the non-radiative transitions of the  ${}^6I_{7/2}$  term level are to the  ${}^6P_J$  term levels. The error in the transition probabilities is about 10% and is mainly due to the error in the relative intensity measurements.

Class		I	II
${}^6P_{7/2}^{(\mu)}$ (in $cm^{-1}$ )	$\mu = 1$	32070	31987
	$\mu = 2$	32082	31032
	$\mu = 3$	32113	32095
	$\mu = 4$	32154	32154
Barycentre ( $cm^{-1}$ )		32105	32067
CF splitting ( $cm^{-1}$ )		84	167
$r^{(\mu)} = r$		0.04	0.05
$\tau^{-1}$ (in ms)		9.2	9.5
$A_{sp}^{(1)}$ (in $s^{-1}$ )		105	100
$A_{vib}^{(1)}$ (in $s^{-1}$ )		4	5
${}^6I_{7/2}^{(\mu)}$ (in $cm^{-1}$ )	$\mu = 1$	35741	35782
	$\mu = 2$	35787	35764
	$\mu = 3$	35845	35787
	$\mu = 4$	35878	35862
Barycentre ( $cm^{-1}$ )		35813	35779
CF splitting ( $cm^{-1}$ )		137	160
$\tau^{-1}$ (in ms)		2.8	2.6
$A_{sp}^{(1)}$ (in $s^{-1}$ )		259	279
$A_{nr}^{(1)}$ (in $s^{-1}$ )		98	106

The excitation spectra in the  ${}^8S_{7/2} \rightarrow {}^6I_{7/2}$  region of the main  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission lines are given in figure 4. The two excitation spectra differ significantly. The lines at 35702, 35764 and 35862  $cm^{-1}$  occurring in the excitation spectrum of class II, figure 4(b), do not occur in the excitation spectrum of class I, figure 4(a). The excitation spectra of the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  emission line at 35702  $cm^{-1}$  is equal to the excitation spectrum of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission line of class II. The excitation spectra of the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  emission line at 35741  $cm^{-1}$  is equal to the excitation spectrum of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission line of class I. The emission lines in the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  region can thus be assigned to the two sites as in figure 2.

Now that we know that at 4.2 K energy transfer occurs from class I to class II and that the CF splitting of class II is the largest we are able to assign the lines in figure 4. The positions and assignments are tabulated in table 1. The total CF splitting of the  ${}^6I_{7/2}$  term level of  $Gd^{3+}$  in class I (II) is 137 (160)  $cm^{-1}$ .

It is possible to excite class II selectively by tuning the excitation to 35702  $cm^{-1}$ . A single emission line is now observed. The decay curve at 4.2 K shows a build up

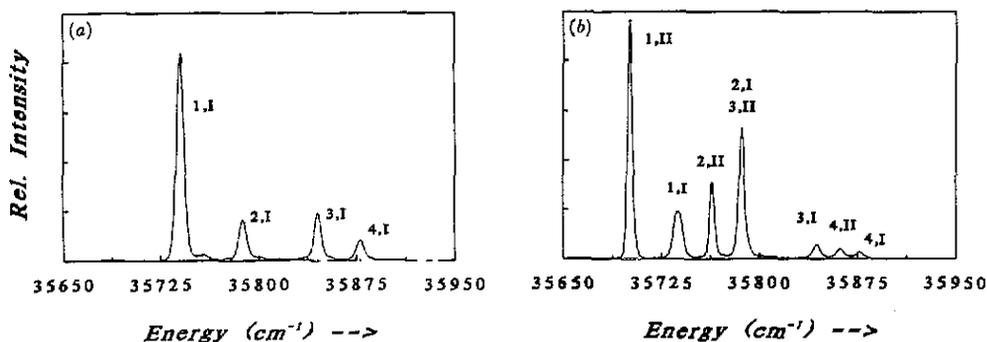


Figure 4. Excitation spectrum in the  ${}^8S_{7/2} \rightarrow {}^6I_{7/2}$  region of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission of the two classes of sites of  $Gd^{3+}$  in  $KYF_4$  at 4.2 K. (a) is for emission from class I, (b) is for emission from class II. The lines are labelled with the CF component index and the class number.

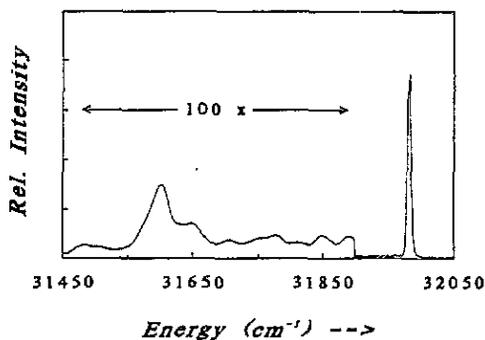


Figure 5. Emission spectrum of the  ${}^6P_{7/2}^{(1)} \rightarrow {}^8S_{7/2}$  transition of  $Gd^{3+}$  in class II in  $KYF_4$  at 4.2 K. Excitation is at  $35702\text{ cm}^{-1}$ . On the right-hand side of the spectrum is the zero-phonon line; at lower energies vibronic lines are observed.

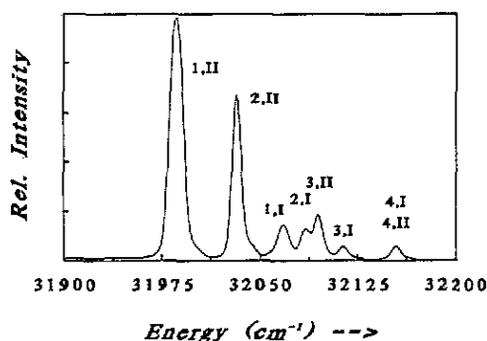


Figure 6. Emission spectrum of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition of  $Gd^{3+}$  in  $KYF_4$  at 62 K, after excitation at  $35702\text{ cm}^{-1}$ . Despite selective excitation of class II, emission is also observed from class I. The lines are labelled with the CF component index and the class number.

due to feeding from the  ${}^6I_{7/2}^{(1)}$  CF component. The superscript (1) indicates the CF component index. The tail of the curve is exponential with a decay time  $\tau_{II} = 9.5\text{ ms}$ . Coupling of the purely electronic transition to crystal lattice vibrations is observed via the occurrence of vibronic lines (figure 5). The strongest vibronic line is at  $\approx 380\text{ cm}^{-1}$  from the zero-phonon line. This is a regular value for the phonon energy in a fluoride compound [9]. The ratio  $r_{II}$  of the integrated vibronic intensity to the integrated zero-phonon intensity amounts 0.05. Non-radiative transitions to the ground state can be neglected at 4.2 K and energy migration over the  $Gd^{3+}$  ions of class II to quenchers does not occur. We then have that the ratio  $r_{II}$  is equal to the ratio of the vibronic transition probability  $A_{\text{vib},II}^{(1)}$  and the zero-phonon transition probability  $A_{\text{zp},II}^{(1)}$  [12]. Here, the superscript indicates that these are values for the first CF component. The

subscript represents the class index. We find  $A_{z_p,II}^{(1)} = 100 \text{ s}^{-1}$  and  $A_{vib,II}^{(1)} = 5 \text{ s}^{-1}$ .

It is not possible to excite in such a way that only emission from class I is observed. To obtain the value of  $r$  for the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition of  $Gd^{3+}$  in class I, we excite the sample at  $35845 \text{ cm}^{-1}$ . We define  $R$  as the ratio of the zero-phonon intensities of classes II and I, and  $r_{I+II}$  as the ratio of the total vibronic intensity to the total zero-phonon intensity. The value of the integrated vibronic intensity to the integrated zero-phonon intensity occurring from class I is then given by  $r_I = r_{I+II}(1 + R) - r_{II}R$ . This yields  $r_I = 0.04$ . The decay curve of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition of  $Gd^{3+}$  in class I also shows an initial build up. The exponential tail has a decay time of  $\tau_I = 9.2 \text{ ms}$ .

The occurrence of energy transfer from class I to class II means that  $\tau_I^{-1}$  equals the sum of the radiative transition probability,  $A_{r,I} = A_{z_p} + A_{vib}$ , and the energy transfer transition probability,  $A_{I-II}$ . We note that the decay times of the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition do not differ much for the both classes. For  $Gd^{3+}$  in a fluoride compound it is expected that this transition has only a magnetic dipole contribution (see later). The radiative transition probabilities are henceforth expected to be the same for both classes. Clearly, the extra decay path for class I by energy transfer to class II does not speed up the relaxation of class I considerably. The ratio of  $A_{I-II}$  to  $A_{z_p,I}$  equals the ratio of the total emission intensity of class II to the total emission intensity of class I (after excitation in one of the CF components of class I):  $A_{I-II}/A_{z_p,I} = R \cdot (1 + r_{II})/(1 + r_I)$ . With  $R = 0.26$  the radiative transition probabilities for the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition of  $Gd^{3+}$  in class I are estimated to be  $A_{z_p,I}^{(1)} = 83 \text{ s}^{-1}$  and  $A_{vib,I}^{(1)} = 3 \text{ s}^{-1}$ . The energy transfer probability equals  $A_{I-II} = 22 \text{ s}^{-1}$ .

No vibronic lines are observed for the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  transition. The decay time  $\tau$  of this transition is 2.8 and 2.6 ms for classes I and II, respectively. The  ${}^6I_{7/2}^{(1)}$  CF component decays via a radiative process to the  ${}^8S_{7/2}$  ground state and via a non-radiative process to the  ${}^6P_J$  term levels. After the non-radiative decay, the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition takes place. For the  ${}^6I_{7/2}^{(1)}$  CF component, therefore,  $\tau^{-1}$  equals the sum of the radiative,  $A_{z_p}^{(1)}$ , and non-radiative,  $A_{nr}^{(1)}$ , transition probability. For  $Gd^{3+}$  in class II an additional non-radiative decay route exists via energy transfer to  $Gd^{3+}$  in class I. This will be incorporated in the value of  $A_{nr}$ . The ratio of the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  emission intensity to the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  emission intensity yields the ratios of the radiative and non-radiative transition probabilities. The intensity ratio is measured as the density of photons. Thus we can derive the separate values of  $A_{z_p}^{(1)}$  and  $A_{nr}^{(1)}$  for transitions starting from the  ${}^6I_{7/2}^{(1)}$  term level, for both classes of sites. The values are given in table 1.

With increasing temperatures the higher CF components of the term levels are also observed in emission (figure 6). After excitation at  $35702 \text{ cm}^{-1}$ , i.e. selective excitation of site II, and at temperatures above 25 K, the emission lines of site I are also observable (figure 6).

#### 4. Discussion

From the emission spectra at 4.2 K, figures 1 and 2, we conclude that there are two different classes of site, I and II. To summarize the differences between the classes, we

note that the barycentre of the CF components is lowest and the CF splitting and the inhomogeneous broadening are largest for class II. The lower position of the barycentre means that sites in class II are the more covalent sites.

In the crystal structure we also distinguish two different classes of cation sites: (a) cation sites that are occupied either by a rare earth ion or by  $K^+$  according to a fixed statistical distribution; and (b) sites that are occupied by a rare earth ion ( $Y^{3+}$  or  $Gd^{3+}$ ). We now try to bring the spectroscopical and crystallographical classification into agreement. Therefore we note that in the first coordination sphere, cations in both classes are surrounded by  $F^-$  ions in a slightly distorted fluorite arrangement. In their second coordination sphere, cations in class (b) [(a)] have mainly cations in class (a) [(b)]. The statistical distribution of  $K^+$  and rare earth ions over the sites in class (a) hence yields the more inhomogeneous environment for sites in class (b). Moreover, the presence of  $K^+$  in class (a) increases the covalency of  $Gd^{3+}$  on a site in class (b). We thus conclude that class II corresponds to class (b) and that class (I) corresponds to class (a).

The assignment is confirmed by the emission spectrum at 4.2 K in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition region after low resolution excitation. For this, we first note that in a unit cell there are twelve rare earth ions belonging to class (b) and six rare earth ions in class (a) (see section 2.1). The radiative transition probabilities are of the same order of magnitude for the two classes. Therefore, the emission of  $Gd^{3+}$  in class II will be strongest after low resolution excitation, i.e. equal excitation intensity for both classes. We measured the emission spectrum in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition region on the MPF-44B spectrofluorometer. It is found that the class II emission has a larger intensity than the class I emission. This confirms that class (II) corresponds to class (b).

The positions of the  ${}^6P_{7/2}$  and the  ${}^6I_{7/2}$  term levels are in good agreement with positions found in other fluorides [7, 13, 14]. Vibronic lines are observed in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transitions and are not observed in the  ${}^6I_{7/2} \rightarrow {}^8S_{7/2}$  transition, in accordance with theory [15, 9]. The vibronic intensity ratios,  $r_I$  and  $r_{II}$ , and the transition probabilities are of a magnitude comparable with values found for  $LaF_3 : Gd^{3+}$  and  $LiYF_4 : Gd^{3+}$  [9].

The rare earth zero-phonon transitions have, in general, a forced electric-dipole (forced ED) and a magnetic-dipole contribution. The magnetic-dipole (MD) contribution to the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition is  $122 \text{ s}^{-1}$  [16, 12]. The measured zero-phonon transition probability is even smaller than this value. Apparently, practically no ED contribution is present in the  ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$  transition. Since the sites have no inversion symmetry, this is ascribed to the high position of the opposite parity states ( $\gtrsim 75000 \text{ cm}^{-1}$  [17]). Mixing of opposite parity configuration into the  ${}^6P_{7/2}$  wavefunctions is therefore negligible. The theoretical value of  $122 \text{ s}^{-1}$  for the MD transition probability is the average value over the equally populated CF components. Our measured values are the probabilities from the lowest CF component. This may account for the difference between the theoretical value and our measured value. It cannot be excluded that the decay times are influenced by retrapping of emission in the crystal. If retrapping occurs, the true radiative transition probabilities will be slightly larger than the values presented here.

In order to measure the contributions of the other CF components, one should measure the intensity of the  ${}^6P_{7/2}^{(\mu)} \rightarrow {}^8S_{7/2}$  zero-phonon transition relative to the intensity of the  ${}^6P_{7/2}^{(1)} \rightarrow {}^8S_{7/2}$  zero-phonon transition as a function of temperature

[12, 9]. We could not do so, since the  ${}^6P_{7/2}$  term levels of the two  $Gd^{3+}$  sites have a spectral overlap.

Above 25 K energy transfer also occurs from class II to class I (figure 6). An accurate analysis of this migration process is beyond the scope of this article.

In conclusion, we have studied the spectroscopy of  $KYF_4$  doped with 5 at.%  $Gd^{3+}$ . Evidence is given that  $Gd^{3+}$  occupies two classes of sites in the crystal lattice. At 4.2 K energy transfer occurs from class I to class II. Above 25 K, energy transfer also occurs vice versa.

### Acknowledgments

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